

Supplementary Text : Comparison of different fits to the pair-correlation data

We fitted the data for $C_z(r)/C_z(0)$ vs r with the following functions: i) $1-ar$ (a is the fitting parameter), ii) $1-ar^\theta$ (a and θ are the fitting parameters), iii) $\exp(-ar)$ (a is the fitting parameter), iv) $\exp(-ar^\theta)$ (a and θ are the fitting parameters). For the functions in (iii) and (iv) the fitting was carried out in the semi-log space ($\log(C_z(r)/C_z(0))$ vs r). The first 15 data points (from $r=0$ to $r=1.5\mu\text{m}$) in $C_z(r)$ were used in estimating the fitting parameters. The fitting was carried out using the nonlinear least squares (nls()) function in the R statistical package. We computed the sum of the square residuals (SSR) and evaluated the corrected Akaike Information Criterion (AIC_c) defined as, $AIC_c = 2m + n \ln(SSR/n) + 2m(m+1)/(n-m-1)$ ¹, where m is the number of fitting parameters and n ($=15$) is the number of data points used in the fits. The difference of the AIC_c ($(\Delta AIC_c)_i = (AIC_c)_i - (AIC_c)_{\min}$) between a pair of fitting functions (denoted as i and j , where function or model j possesses the minimum AIC_c value $(AIC_c)_{\min}$ in the pair i,j) provides an information theoretic way to discriminate between the ability of these functions to describe the data. The AIC_c values can be used to rank the models in their ability to describe the data¹, e.g., the model corresponding to the lowest AIC_c is best model compared to the other models. If the competing model has an AIC_c value higher than <2 points compared to the best model, the competing model cannot be discriminated well from the best model; if the competing model has an AIC_c value above 9-11 or above 20, the model has little support or has no support. The following tables (Table S1) show the fitting functions and the corresponding AIC_c values. The models with the lowest AIC_c values are marked with green colored rows. The ΔAIC_c values indicate that the data convincingly support the a non-linear decay ($1-ar^\theta$) (Table S1A and Figure S1) or a non-exponential decay ($\exp(-ar^\theta)$) (Table S1B and Figure S2) of the correlation function $C_z(r)/C_z(0)$. The fits to the data are shown in Figures S1 and S2.

References

1. Burnham KP, Anderson DR, Huyvaert KP. AIC model selection and multimodel inference in behavioral ecology: some background, observations, and comparisons. Behavioral ecology and sociobiology 2011;65:23-35.